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N^o. XLI.

Calculations relating to Grist and Saw Mills, for determining the quantity of Water necessary to produce the desired effect when the Head and Fall are given in order to ascertain the dimensions of a new invented Steam Engine, intended to give motion to Water-wheels in places where there is no Fall, and but a very small Stream or Spring.
By JOHN NANCARROW.

ELEMENTS used in the following calculations, so far as they relate to works moved by water-wheels :

1. let h = mean height of the head of water in the penstock.
2. a = the area of the aperture or gateway.
3. $q = 6.128$ = the number of ale gallons in a cubic foot.
4. $s = 16$ feet, = the space a heavy body falls from rest in one second.
5. $2s$ = the uniform velocity acquired by falling 16 feet from rest.
6. $2\sqrt{hs}$, or $8\sqrt{h}$ = the uniform velocity acquired by falling from rest any depth = h .
7. $8aq\sqrt{h}$, the number of ale gallons issuing through any aperture a in one second, and $8aqt\sqrt{h}$ = the quantity in t seconds.
8. $8a\sqrt{h}$ = the number of cubic feet flowing through a in one second, and $8at\sqrt{h}$ = the number of cubic feet in t seconds.
9. $w = 62.5$ pounds avoirdupoise, = the weight of a cubic foot of water, and 10.2 lbs. = the weight of an ale gallon.
10. haw = the weight of any column of water.
11. $\frac{\sqrt{h}}{4} = t$ = the time of falling from an height = h .
12. $D - \frac{d}{2}$ is the common practical rule for finding the mean height of the head of water when the aperture is vertical and rectangular where D represents the depth of

of water in the penstock, and d the height of the gateway, and is only an approximation, though very near the truth; the genuine method derived from the parabola is as follows:

Let ABCD Fig. 1. represent a large cistern or penstock, and MKLN an orifice made in one of its sides.

When the upper edge of the gateway, as KL is below the surface of the water in the penstock, the sum of all the velocities or sheets of water which flow through it, being expressed by the elements of the segment of a parabola FHIG, there will be found amongst them a mean ordinate OT, which being multiplied by the height HP, will give a product equal to the area of this segment. Now, in order to determine the mean height EO, let EP= a , EH= b , HP= c , and the mean height EO= x . The sum of all the velocities, or the area of the parabola EPG will be $\frac{2a}{3}\sqrt{a}$, and the sum of all the velocities acquired by

falling from E to H = $\frac{2b}{3}\sqrt{b}$; consequently $\frac{2a}{3}\sqrt{a} - \frac{2b}{3}\sqrt{b}$ will give the sum of all the velocities which flow through the orifice MKLN, which is equal to the parabolic segment HPIG, or to the product of the mean velocity \sqrt{EO} (x) by the height HP (c), hence we have $\frac{2a}{3}\sqrt{a} - \frac{2b}{3}\sqrt{b} = c\sqrt{x}$, which equation being reduced will give $x = \frac{4}{9} \times \frac{a^3 + b^3 - 2ab\sqrt{ab}}{cc}$.

E X A M P L E.

If the height EP (a) be = 8 feet, EH (b) = 6 feet, then will HP or c = 2 feet; and by substituting these numbers for their respective values in the above equation, x will be found = 6.99 feet.

By the common practical rule, (see article 12,) $D - \frac{d}{2} = h = x$, where $D=8$ and $d=2$; consequently $h = 7$ feet, whence it appears that $a - \frac{c}{2} = D - \frac{d}{2}$ is sufficiently exact for all common purposes.

In

In the foregoing elements (see art. 4 and 5.) I have supposed the space which a heavy body describes by falling from rest in one second of time to be 16 instead of $16\frac{1}{4}$ feet, and the uniform velocity acquired by such fall = 32 feet; whereas every author which I have read, (even on the subject of hydraulics) makes it $32\frac{1}{2}$ feet, without allowing for the friction the water is subjected to in its passage through the aperture or gateway, or for the resistance it meets with by its sudden impulse against the air, immediately on its leaving the penstock. It evidently follows that the uniform velocity must be diminished on both these accounts: hence we may safely conclude, that a uniform velocity of 32 feet in one second, will be found to coincide with an experimental proof, nearer than that of $32\frac{1}{2}$ feet in the same time.

Before the dimensions of the steam engine can be ascertained, it is essentially necessary to know what quantity of water it must deliver into the penstock in a given time, in order that the power or force by which the water-wheel is moved, may be at least adequate to the purpose intended. Several grist and saw-mills have been examined with this view, and such measurements carefully taken as were thought necessary for determining the powers by which they are moved. Amongst these we have selected John Beydler's grist and saw-mills, and a saw-mill belonging to Christopher Keyger, both in the county of Berks and state of Pennsylvania.

Calculation of the power applied to Beydler's grist-mill, either for one or two pair of stones, each being $4\frac{1}{2}$ feet in diameter, and that of the water-wheel 16 feet; the top of which is nearly on a level with the bottom of the penstock, and grinds from 50 to 60 bushels of wheat in 12 hours, with a single pair of stones.

THE head or depth of water from its surface to the bottom of the penstock for working one pair of stones = 22 inches.

The gateway or aperture a is 30 inches wide by $1\frac{1}{2}$ inch deep = 45 inches = 0.3125 parts of a square foot.

Mean height of the head, or $D - \frac{d}{2} = b$ (art. 12.) = $21\frac{1}{4}$ inches = 1.77 feet.

By art. 7th we have $8aq\sqrt{b}$ = the number of ale gallons issuing through any aperture a in one second, = $8 \times 0.3125 \times 6.128$

$6.128 \times 1.33 (\sqrt{b}) = 20.38$ gallons of water flowing through the gateway in one second of time. The number of cubic feet which issue through this aperture in the same time $= 8a\sqrt{b}$ (art. 8.) $= 8 \times 0.3125 \times 1.33 = 3.325$, which being multiplied by 62.5 pounds, the weight of a cubic foot of water, gives 207.8 lbs. for the whole pressure on the upper part of the wheel during the space of one second; but the instantaneous pressure, or force of impact, where the water first strikes the wheel, is *haw* (art. 10.) $= 1.77 \times 0.3125 \times 62.5 = 34.57$ pounds; also $8\sqrt{b}$ = the uniform velocity acquired at *a* the aperture in a second, $= 10.64$ feet.

When this mill drives two pair of stones, the gate is raised an half inch higher; *b* being in this case $= 1.75$ and $\sqrt{b} = 1.323$ feet, by which means *a* becomes $= 30 \times 2$ or 60 square inches, $= 0.417$ parts of a square foot. The other measurements remaining the same as above, we shall have

$$8aq\sqrt{b} = 27 \text{ gallons per second,}$$

$$8a\sqrt{b} = 4.414 \text{ cubic feet per do.}$$

$$haw = 46.5 \text{ pounds for the force of impact,}$$

$$\text{and } 8\sqrt{b} = 10.584 \text{ feet for the uniform velocity per second.}$$

In Emerson's Mechanics, and Fletcher's Universal Measurer and Mechanic, the uniform velocity acquired by falling from an height $= b$, is denoted by $\sqrt{2bs}$ instead of $2\sqrt{bs}$, which is the true measure of its celerity. This circumstance is not mentioned with the least view to find fault with these authors, but to remove any doubts which may arise in the minds of such as are disposed to peruse these calculations.

BEYDLER'S SAW-MILL.

This mill has a small undershot wheel, commonly called a flutter wheel, which is no more than 3 feet in diameter. The depth of the water from its surface to the bottom of the penstock is 3 feet, the gateway is 3 feet wide by 6 inches deep, $= 1.5$ square foot, the mean height of the head or D— $\frac{d}{2} = 2.75$ feet $= b$, and $\sqrt{b} = 1.658$. The fall from the bottom of the penstock to the place where the water impinges on the float or ladle-board is 10 feet, and $2.75 + 11 = 13.75$, being equal to the whole height

height of the column of water which propels this wheel. Now by art. 7. we have $8aq\sqrt{h}$ = the quantity of water which flows through the gateway in one second, $= 8 \times 6.128 \times 1.5 \times 1.658 = 121.92$ gallons. Again, $haw = 2.75 \times 1.5 \times 62.5 = 257.8$ pounds, which is equal to the weight of the column pressing against the aperture; also $8\sqrt{h} = 13.264$ feet, the uniform velocity of the water every second as it issues through the gateway.

In order to find the force of impact on the wheel, we must, in the first place determine (what may be called) the initial weight of the water, or that with which it may be supposed to begin to press at its surface in the penstock, viz. by dividing the momentum by the uniform velocity; but $haw = 257.8$ is the momentum at the aperture or gateway, and 13.264 = the uniform velocity: therefore $\frac{257.8}{13.264} = 19.406$ lbs. = W , the initial

weight required $= \frac{haw}{8\sqrt{h}} = \frac{aw}{8} \sqrt{h}$; consequently $8W\sqrt{h}$ will express the force of impact sought, h being now $= 13.75$ and $\sqrt{h} = 3.708$; hence $8W\sqrt{h} = 8 \times 19.406 \times 3.708 = 575.66$ pounds for the constant impelling force on the ladle-board; but $575.66 = haw$, and $a = \frac{575.66}{baw} = \frac{575.66}{13.75 \times 62.5} = 0.67$ parts of a square

foot. To prove the truth of the above method for finding the force of impact, we need only try whether $8aq\sqrt{h}$ (where $h = 13.75$ and $a = 0.67$) will produce the same number of gallons as that before found, viz. 121.9 in one second. In the present case $8aq\sqrt{h} = 8 \times 0.67 \times 6.128 \times 3.708 = 121.8$ being nearly the same as found above, and is a sufficient proof that the force of impact where the water impinges on the wheel is rightly determined.

KEYGER'S SAW-MILL.

This saw-mill is over-shot, the wheel 12 feet diameter, the penstock is 6 feet in depth by 2 feet wide, and when I saw it at work, there were only 4 feet and 1-4th inch of water in the cistern, although the saw moved at the rate of 120 strokes in a minute, whilst it passed through a piece of oak at least 12 inches deep,

deep, and the gateway no more than half an inch high. Hence $h = 4$, and $\sqrt{h} = 2$ feet. The aperture $a = 24 \times 0.5 = 12 = 0.0833$ parts of a square foot; wherefore $8aq\sqrt{h} = 8 \times 0.0833 \times 6.128 \times 2 = 8.2$ gallons which falls on the wheel in the space of one second, $8a\sqrt{h} = 8 \times 0.0833 \times 2 = 1.32$ cubic feet in the same time, and $8\sqrt{h} = 16$ feet, the uniform velocity per second, as the water leaves the aperture; also $haw = 4 \times 0.0833 \times 62.5 = 20.8$ pounds for the force of impact where the water first enters on the wheel. When this mill is supplied with a 6 feet head, and the gate drawn up one inch, the saw makes 180 strokes in a minute through an oak log 18 inches deep. We have now $h = 6$, $\sqrt{h} = 2.45$ feet, and $a = 24$ inches $= 0.167$ parts of a square foot. Here $8aq\sqrt{h} = 8 \times 0.167 \times 6.128 \times 2.45 = 20$ gallons per second, $8a\sqrt{h} = 8 \times 0.167 \times 2.45 = 3.273$ cubic feet in the same time, and $8\sqrt{h}$ = the uniform velocity acquired by a fall of 6 feet; also $haw = 6 \times 0.167 \times 62.5 = 62.6$ for the weight of the column or force of impact on the wheel.

I have been the more particular in making these calculations in order to ascertain the dimensions of the steam-engine for various purposes; on which account we must again have recourse to the parabola, and also to the inverted syphon.

To find the retarded velocity and time of ascent of water into an exhausted receiver, through a vertical pipe or tube, by the assistance of the parabola. Fig. 2.

Let CBBG be an inverted syphon, the diameter being every where equal, accompanied with a cock T, and the first branch AE always kept full of water: it is certain that if all the rest of the syphon be empty, and the cock be suddenly opened, the water will immediately rush into the tube of communication VX with a uniform velocity equal to that which a heavy body would acquire by falling from A to B, and will be continually diminished in proportion as the second branch is filled.

To shew in what order this retardation of the water diminishes its velocity at any point Q of the tube GS, where it is supposed to be ascending towards *qr*, we must describe on the lines AB, CD as an axis with the same parameter, two equal parabolas CPH and BKI, situated in opposite directions. Complete the parallelogram AM, and draw as many lines LR as

you please parallel to the horizontal line IG. Now if we take the ordinate AI, or its equal DH to express the whole uniform velocity acquired by falling from C to D, it is evident that the ordinate OP will denote the velocity at the point O, acquired by a fall equal to CO, and the ordinate NK will express the velocity arising from a fall equal to NB or QS. But we shall prove that the velocity of the ascending water in the second branch, when it arrives at Q, ought not to be expressed by the ordinate which corresponds to it; but by the line LK, the difference between the entire uniform velocity LN or MB (by falling from A to B) and that of NK.

To demonstrate that the height QS or NB of the water in the tube SR, is equal to a fall which can produce the relative velocity arising from CD, or the difference between the velocities acquired by falling from A to B, and that of the ascending water at Q; let AB and QS be considered as two non-elastic bodies, whose momenta are as the altitudes AB and QS. If $AB = a$ and $QS = r$, we shall have $a = \sqrt{a} \times \sqrt{a}$, and $r = \sqrt{r} \times \sqrt{r}$; but the difference of the momenta divided by the sum of the bodies is equal to the velocity, which let be v ; therefore

$\sqrt{a} \times \sqrt{a} - \sqrt{r} \times \sqrt{r}$ divided by $\sqrt{a} + \sqrt{r} = \frac{\sqrt{a} + \sqrt{r} \times \sqrt{a} - \sqrt{r}}{\sqrt{a} + \sqrt{r}} = \sqrt{a} - \sqrt{r} = v = LK$, the velocity of the water at Q, and $\sqrt{a} - v = \sqrt{r}$, which is the relative velocity produced by a fall equal to QS. As this velocity is expressed by the ordinate NK, the difference between it and MB or LN will express the retarded velocity of the water in the tube of communication DX, which is the same as that of the surface QR at the point Q.

As it will be the same with all the retarded velocities during the time employed in filling the tube GF, it follows that their sum will be expressed by that of all the ordinates, or the area of the parabolic complement MIKB.

Before the observations of Belidor on the inverted syphon, in his theory relating to the common sucking pump, it was customary to estimate this sum by the area of the parabola DCPH or ABKI; for the velocity at Q was expressed by the square root of CO, instead of the difference between the square roots of CD and QS.

The parabolic complement MIKB, being but half of the parabola ABKI, it is evident that the sum of all the retarded velocities

velocities in filling the second branch will be no more than half the sum of the velocities on which we have been accustomed to count; from whence it follows that the branch FG will require twice the time to be filled as was formerly imagined. It follows also, that because the complement MIKB, is but one-third of the parallelogram AIMB; therefore the branch BF will be three times as long in filling as it would be with the uniform velocity expressed by MB. And lastly it follows, that the sum of the velocities of water ascending from Q to q, instead of being expressed by the area of the mixed quadrilateral PO *op*, ought to be expressed by the area of the quadrilateral KL *lk*, which may be found in the following manner.

Let AB = *a*, AB = *b*, NB = *r* and *nN* = *c*. Now the uniform velocities being as the ordinates, we shall have AI = \sqrt{a} , nk = \sqrt{b} , NK = \sqrt{r} , and let $b - r = c$; but $\frac{2b}{3}\sqrt{b} - \frac{2r}{3}\sqrt{r}$ = the segment *nNkk*, and $c\sqrt{a}$ = the parallelogram L*Nnl*; consequently $c\sqrt{a} - \frac{2b}{3}\sqrt{b} + \frac{2r}{3}\sqrt{r}$ = the space L*Kkl*, or the sum of all the retarded velocities during the ascent from Q to q.

To give an example in numbers, we will suppose *a* = 30, *b* = 24, *r* = 20 and *c* = 4, then $8\sqrt{a} = 43.82$, $8\sqrt{b} = 39.19$, and $8\sqrt{r} = 35.78$; hence $4 \times 43.82 - \frac{2 \times 24}{3} \times 39.19 + \frac{2 \times 20}{3} \times 35.78 = 175.28 - 627.04 + 477.07 = 25.31$; but by the laws of accelerated motion, the spaces described are as the squares of the times of description; wherefore $32 : 1'' : : 25.31 : 0.79$ and $\sqrt{0.79} = 0.89$ = the time required for the water to ascend from Q to q = 4 feet.

DESCRIPTION OF THE STEAM-ENGINE. Fig. 3.

- A. The receiver, which may be made either of wood or iron.
- BBBBB. Wooden or cast-iron pipes for conveying the water to the receiver and from thence to the penstock.
- C. The penstock or cistern.
- D. The water-wheel.

- E. The boiler, which may be either iron or copper.
- F. The hot-well for supplying the boiler with water.
- GG. Two cisterns under the level of the water, in which the small bores BB, and the condenser are contained.
- HHH. The surface of the water with which the steam-engine and water-wheel are supplied.
- aa. The steam-pipe, through which the steam is conveyed from the boiler to the receiver.
- b. The feeding-pipe for supplying the boiler with hot water.
- cccc. The condensing apparatus.
- dd. The pipe which conveys the hot water from the condenser to the hot-well.
- eee. Valves for admitting and excluding the water.
- ff. The injection pipe, and g the injection cock.
- h. The condenser.

It does not appear necessary to say any thing here on the manner in which this machine performs its operations without manual assistance, as the method of opening the cocks by which the steam is admitted into the receiver and condensed, has been already well described by several writers. But it will be necessary to remark that the receiver, penstock, and all the pipes, must be previously filled before any water can be delivered on the wheel, and when the steam in the boiler has acquired a sufficient strength, the valve at *c* is opened and the steam immediately rushes from the boiler at E into the receiver A, the water descends through the tubes A and B, and ascends through the valve *e* and the other pipe or tube B into the penstock C. This part of the operation being performed and the valve *c* shut, that at *a* is suddenly opened, through which the steam rushes down the condensing pipe *c*, and in its passage meets with a jet of cold water from the injection cock g by which it is condensed. A vacuum being made by this means in the receiver, the water is driven up to fill it a second time through the valves *ee* by the pressure of the external air, when the steam-valve at *c* is again opened and the operation repeated for any length of time the machine is required to work.

There are many advantages which a steam-engine on this construction possesses beyond any thing of the kind hitherto invented; a few of which I shall beg leave to enumerate.

1. It is subject to little or no friction.
2. It may be erected at a small expence when compared with any other sort of steam-engine.
3. It has every advantage which may be attributed to Bolton and Watt's engines, by condensing out of the receiver, either in the penstock or at the level of the water.
4. Another very great advantage is, that the water in the upper part of the pipe adjoining the receiver, acquires a heat by its being in frequent contact with the steam, very nearly equal to that of boiling water; hence the receiver is always kept uniformly hot as in the case of Bolton and Watt's engines.
5. A very small stream of water is sufficient to supply this engine, (even where there is no fall) for all the water raised by it is returned into the reservoir HHH.

From the foregoing reasons it manifestly appears that no kind of steam-engine is so well adapted to give rotatory motion to machinery of every kind as this. Its form is simple, and the materials of which it is composed are cheap; the power is more than equal to any other machine of the kind, because there is no deduction to be made for friction, except on account of turning the cocks which is but trifling.

Its great utility is therefore evident in supplying water for every kind of work performed by a water-wheel, such as grist-mills, saw-mills, blast-furnaces, forges, &c.

Dimensions of the Steam-Engine for working an overshot wheel, accompanied with such calculations as are necessary for ascertaining the sizes of its different parts, when applied to various purposes.

The quantity of water which this machine is intended to raise into the receiver in a given time, cannot be ascertained until some standard be fixed on for the height of the surface of the water in the receiver above that in the reservoir HHH, which when known, we shall be enabled to calculate the diameters of the receiver and pipes with certainty.

Writers on the subject of hydraulics generally allow that a column of water 34 feet high is equal to the pressure of the atmosphere when the mercury in the barometer stands at 29.5 inches. Now if we admit that the water will ascend into an exhausted
receiver

receiver to the height of 30 feet only instead of 34 feet, we shall by this means allow about 4 feet for the imperfection of the vacuum, or nearly one-eighth part of the whole power of the machine, if the steam in the receiver could be perfectly condensed. Let therefore the highest elevation of the water in the receiver be 24 feet above the surface of the water in the reservoir, and if the bottom of the receiver and the upper part of the cistern or penstock be each 20 feet above the same level, the diameter of the water-wheel may be easily ascertained when the depth of the penstock or head of water is given.

Now as the velocity of the water is continually retarded during the time employed to fill the receiver, we must again have recourse to the inverted syphon (Fig. 2.) in order to determine the time in which it may be filled and emptied, which when ascertained, we shall be enabled to calculate the number of strokes the machine may make in a minute, and consequently the quantity of water it will deliver on any overshot water-wheel in a given time.

The example on page 355 was purposely intended to shew the time necessary for filling the receiver according to the above dimensions, where $a=30$, $b=24$, $r=20$ and $c=4$ feet; whence it appears that it may be filled in 0'.89 to an height of 4 feet above its bottom, or 24 feet above the level of HHH.

The common steam-engine invented by Newcomen and Cawley, when it works to the best advantage, requires the steam to be made about one-tenth stronger than the surrounding air; but that this receiver may be emptied with sufficient dispatch, it will be necessary to increase the elasticity of the steam at least one-fourth part beyond what is produced from the usual heat of boiling water. Admitting therefore that a column of water 34 feet in height be in equilibrio with the pressure of the atmosphere, we have $\frac{34}{4}=8.5$ feet, which added to 24, the highest elevation of the water above the surface of that in the reservoir, gives 32.5 for the space AB. Fig. 2. There being now but a column of 24 feet instead of 30 as before, pressing against a counteracting column of 20 feet, the descent of the water in the receiver will be considerably slower than its ascent, during the time occupied in filling it to an height of 4 feet above its bottom;

bottom ; but we have supposed the increased elasticity of the steam to be equal to a column of water 8.5 feet high, which being added to 4 feet, the difference between the two columns, makes nB in this case = 12.5 feet, $An = 8.5$ feet, $nN = 4$ feet, and $NB = 4.5$ feet. By these measurements the parallelogram $NnLL$ will be found = 113.1368, the parabola $BnkB = 132.1648$, and the parabola $BNKB = 50.9118$; hence $BnkB - BNKB = NnkK = 81.253$; but $113.1368 - 81.253 = 31.8838 = KkLL$, and $\sqrt{\frac{31.8838}{32}} = 0'.99$ or $1'' =$ the time required to empty the

receiver, when filled with 4 feet of water ; and as it appears that it may be filled in $0'.89$ or $0''.9$ of a second, it is therefore evident that this machine may make 30 strokes in a minute, supposing the pipes and receiver were all of the same diameter ; but it is not necessary that it should exceed 10 strokes per minute, and consequently the pipes which convey the water to and from the receiver, need not be more than one-third part of its area, and on no occasion to exceed one half.

It has been supposed, in what we have said concerning the steam-engine, that the upper part of the penstock is on the same level with the bottom of the receiver, or 20 feet above the level of the water in the reservoir, and admitting the penstock to be 4 feet in depth, (instead of 22 inches, see page 350) there will be a space equal to 16 feet left for the diameter of the wheel ; but that its motion may not be interrupted by wading through the water in the reservoir, we have here supposed the diameter to be no more than 15 feet. Now, if each revolution of the wheel be performed in the time this machine makes one stroke, the circumference must move with a velocity equal to 7.854 feet in each second of time, admitting the steam-engine works at the rate of 10 strokes in a minute.

Previous to determining the capacity of the receiver, it will not be improper to bring into one point of view, what has already been said on the subject of Beydler's grist-mill and Keyger's saw-mill.

Beydler's grist-mill with one pair of stones, where $b = 1.77$ and $a = 0.3125$.

$8agt \sqrt{b} = 20.38$ in one second, and $8agt \sqrt{b} = 122.28$ gallons, t being

t being 6 seconds. $8a\sqrt{b}=3.325$ cubic feet and $8\sqrt{b}=10.64$ feet, the uniform velocity in one second; also $haw=34.57$ lbs. the force of impact on the wheel.

For two pair of stones, b being $=1.75$ and $a=0.417$.
 $8aq\sqrt{b}=27$ gallons in $1''$ and $8agt\sqrt{b}=162$ gallons in 6 seconds.
 $8a\sqrt{b}=4.4$ cubic feet, $8\sqrt{b}=10.584$ and $haw=46.5$ pounds.

Keyger's saw-mill with a 4 feet head $=b$ and $a=0.0833$.
 $8aq\sqrt{b}=8.2$ and $8agt\sqrt{b}=49.2$ gallons in 6 seconds.
 $8a\sqrt{b}=1.32$ cubic feet, $8\sqrt{b}=16$ feet the uniform velocity in $1''$;
 also $haw=20.8$ lbs. the force of impact.

The same mill with a 6 feet head $=b$ and $a=0.167$.
 $8aq\sqrt{b}=20$, $8agt\sqrt{b}=120$, $8a\sqrt{b}=3.273$, $8\sqrt{b}=19.6$
 and $haw=62.6$ pounds.

If it be intended that the receiver shall contain 122.28 gallons for one pair of stones, and 162 gallons for two pair, we shall find that the former number is equal to a cylinder 4 feet high by 30 inches diameter, and that latter number is equal to one of the same height by 3 feet diameter; but to find the area of the gateway in the penstock, adapted to the steam-engine, which is 4 feet deep instead of 22 inches, we must find an area x for the aperture, which shall discharge as much water in a given time, (which we will suppose to be 6 seconds) as flows through the gateway of Beydler's mill in the same time; making therefore H = the head of water at the steam-engine, and b = that of the grist-mill; also a = the gateway as before, we have $x\sqrt{H}=a\sqrt{b}$, and $x=\frac{a\sqrt{b}}{\sqrt{H}}=0.2078$ for one pair of stones, and

0.2758 for two pair. Now Hxn being to haw nearly in the ratio of 3 to 2 for the difference of the forces of impact, we may safely conclude that receivers of the above dimensions will be amply sufficient for supplying the water-wheel with a power as much superior to Beydler's mill, as the difference between the forces of impact will amount to.

With respect to Keyger's saw-mill we shall only remark, that as the quantity of water passing over the wheel with a 6 feet head, is so nearly equal to that which Beydler's mill requires for one pair of stones, that a receiver of equal dimensions will be found sufficiently large, the penstock of the steam-engine being also 6 feet deep.

It will not be necessary that in any case the boiler should contain more than 6 times as much as the receiver; hence we have for Beydler's mill with one pair of stones, and Keyger's saw-mill with 6 feet head, a receiver = 4 feet by 2.5 diameter = to 122.28 gallons, which multiplied by 6 = about 734 gallons for the contents of the boiler. The receiver for the same grist-mill = 4 feet by 3 feet = 162 gallons, and the boiler = 972 gallons.

In order to prevent the water, whilst the receiver is filling, from striking against its top, it will be necessary that one foot at least be added to its height; so that instead of being 4 feet high as we have hitherto supposed, it should be at least 5 feet.

Fig. 1.

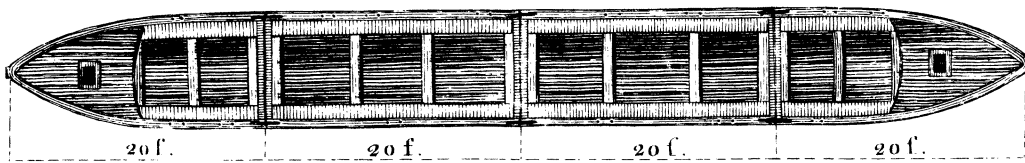


Fig. 2.



Fig. 5.

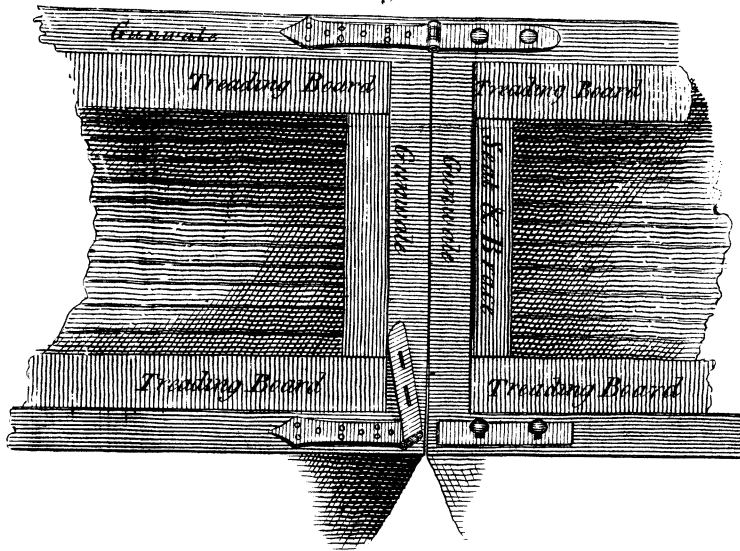


Fig. 3.
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